Supplemental Document

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## Interferometric measurements of nonlinear refractive index in the infrared spectral range: supplement

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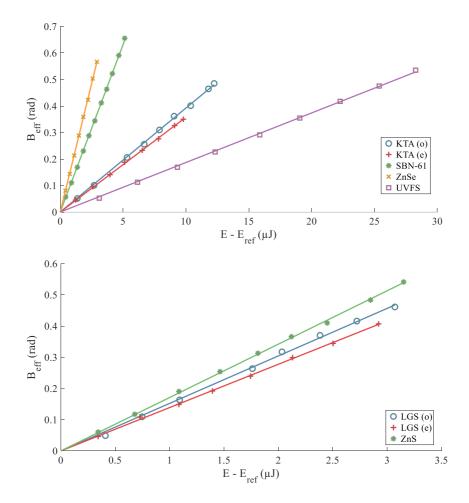
## Interferometric measurements of nonlinear refractive index in the infrared spectral range: supplemental document

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Sample	$I_{lim}$ (1.03 µm) , $rac{\mathrm{GW}}{\mathrm{cm}^2}$	$I_{lim}$ (2.2 $\mu m$ ) , $rac{GW}{cm^2}$	$I_{lim}$ (3.2 $\mu m$ ) , $rac{GW}{cm^2}$
GaSe	-	3.97 - 22.19	4.2 - 18.55
AGS (o)	-	4.18 - 10.96	7.48 - 20.06
AGS (e)	-	4.25 - 11.13	2.58 - 19.84
ZGP (o)	-	3.1 - 8.77	5.48 - 21.24
ZGP (e)	-	2.29 - 8.27	10.16 - 19.07
SBN-61 (o)	0.88 - 6.58	2.91 - 10.31	5.6 - 20.98
KTA (o)	3.23 - 16.45	8.01 - 33.38	5.15 - 21.14
KTA (e)	6.35 - 16.75	8.17 - 26.52	9.3 - 20.56
LGS (o)	0.85 - 4.08	-	5.78 - 15.5
LGS (e)	0.82 - 3.95	2.47 - 9.17	5.35 - 16.09
BGSe	-	4.51 - 9.13	5.69 - 17.3
GaAs	-	1.49 - 7.68	3.27 - 13.85
Si	-	2.07 - 5.96	3.63 - 14.85
ZnTe	-	2.77 - 20.5	6.15 - 19.76
ZnS	0.84 - 4.25	2.68 - 11.85	5.88-21.11
ZnSe	1.35 - 4.38	3.99 - 13.45	7.68-23.52
KRS-5	-	2.58 - 6.11	1.85 - 9.57
KRS-6	-	8.75 - 19.43	5.95 - 20.99
UVFS	7.37 - 34.32		

Table S1. Peak intensity lin	mits <i>I<sub>lim</sub></i> within the sample	le for different $n_2$ measurements.
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07 101		1 2	
$E_{\mathrm{ref}}$ (1.03 µm) , µJ	$E_{ m ref}~(2.2~\mu m)$ , $\mu J$	$E_{ref}~(3.2~\mu m)$ , $\mu J$	
-	2.19	1.05	
-	2.48	2.17	
-	2.56	0.53	
-	1.78	1.31	
-	0.65	3.57	
0.29	1.58	1.5	
1.3	2.35	1.26	
4	2.37	3.11	
0.29	-	1.41	
0.34	1.24	1.68	
-	2.29	1.76	
-	0.57	0.66	
-	0.63	0.55	
-	1.08	1.85	
0.35	0.78	1.17	
0.69	1.72	1.81	
-	1.15	0.29	
-	3.11	1.18	
3.77	-	-	
	Eref (1.03 µm) , µJ - - - - 0.29 1.3 4 0.29 0.34 - - - 0.34 - - 0.35 0.69 - -	Eref (1.03 µm), µJ         Eref (2.2 µm), µJ           -         2.19           -         2.48           -         2.56           -         1.78           -         0.65           0.29         1.58           1.3         2.35           0.29         -           0.29         -           0.29         -           0.29         -           0.29         -           0.34         2.29           -         0.57           -         0.57           -         0.57           -         0.53           -         0.57           -         0.53           -         0.57           -         0.57           -         1.08           -         1.08           0.35         0.78           0.69         1.72           -         1.15           -         3.11	

**Table S2.** Reference energy  $E_{ref}$  within the sample for different  $n_2$  measurements.



**Fig. S1.** Effective total nonlinear phase shift at different energies within the sample for different measurements at 1.03 µm. Dots – experimental points, line – linear fit.

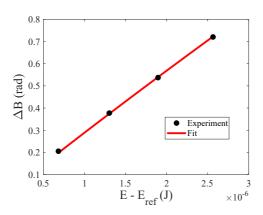


Fig. S2. The change of total nonlinear phase shift at different energies within the Si sample at  $2.2 \,\mu$ m. Dots – experimental points, line – fit.

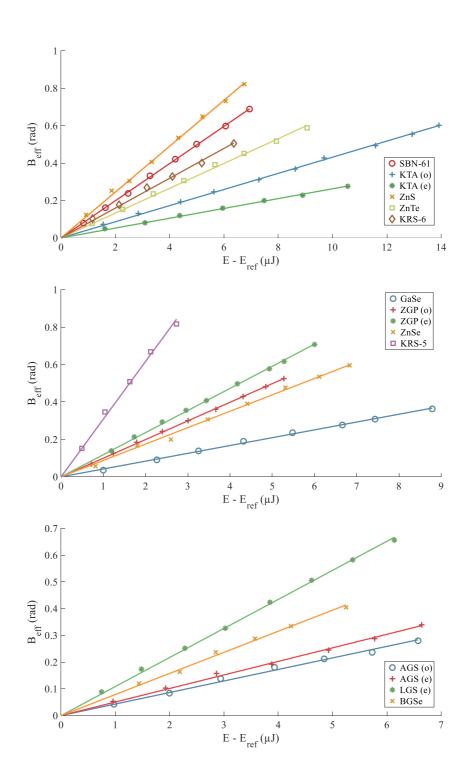
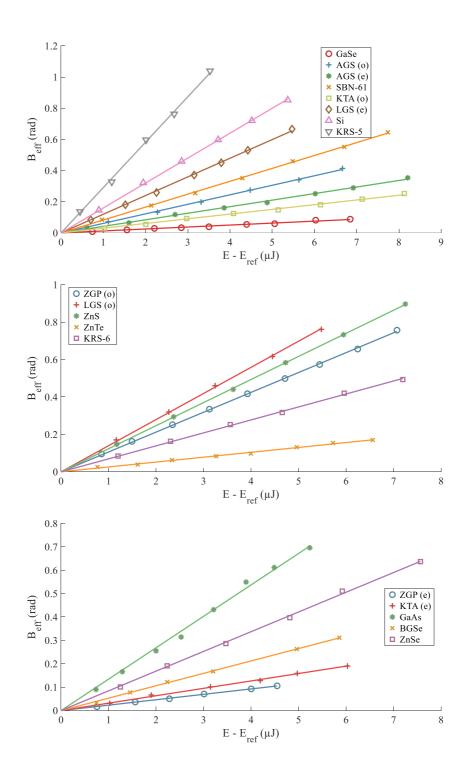
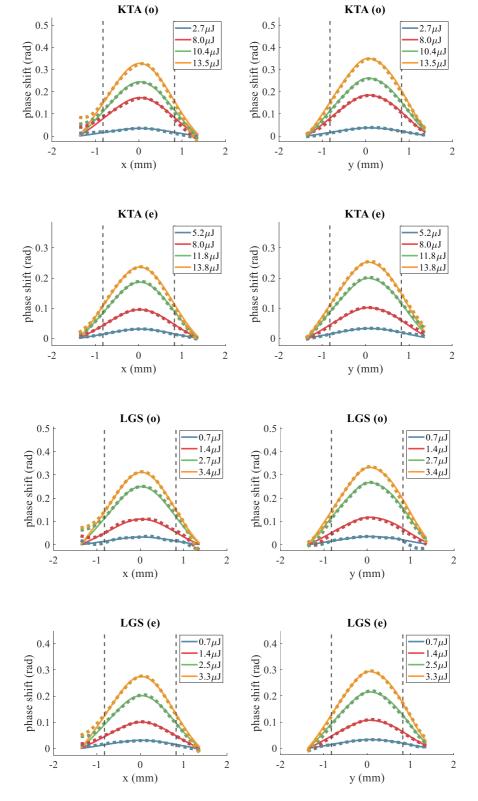


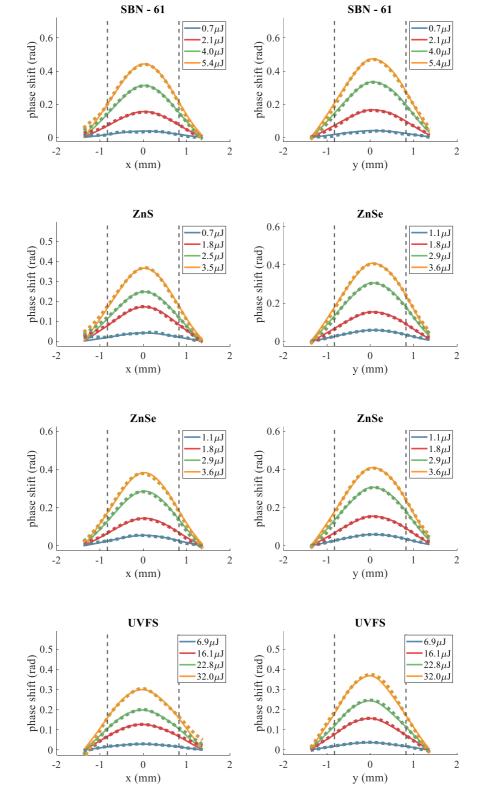
Fig. S3. Effective total nonlinear phase shift at different energies within the sample for different measurements at 2.2  $\mu$ m. Dots – experimental points, line – linear fit.



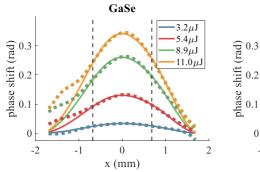
**Fig. S4.** Effective total nonlinear phase shift at different energies within the sample for different measurements at  $3.2 \mu m$ . Dots – experimental points, line – linear fit.

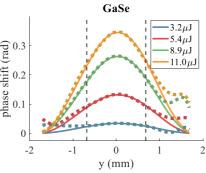


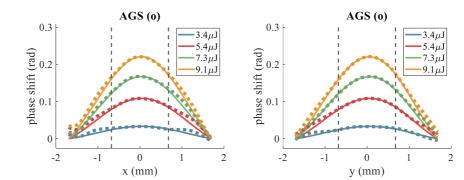
**Fig. S5.** Retrieved X and Y cuts of phase shifts observed in different samples for various laser pulse energies at  $1.03 \mu m$ . Dashed line - data, solid line - approximation. The vertical dashed lines indicate the part of the data included in  $n_2$  estimation.

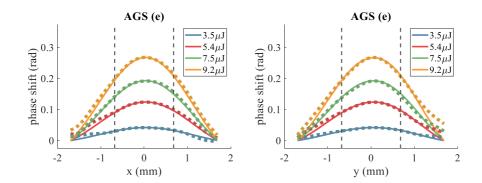


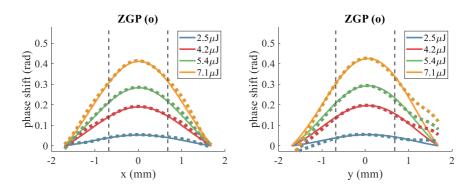
**Fig. S6.** Retrieved X and Y cuts of phase shifts observed in different samples for various laser pulse energies at 1.03  $\mu$ m. Dashed line - data, solid line - approximation. The vertical dashed lines indicate the part of the data included in  $n_2$  estimation.



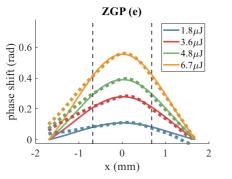


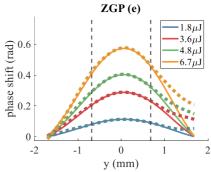






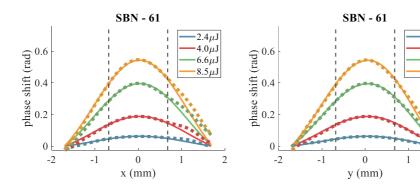
**Fig. S7.** Retrieved X and Y cuts of phase shifts observed in different samples for various laser pulse energies at 2.2  $\mu$ m. Dashed line - data, solid line - approximation. The vertical dashed lines indicate the part of the data included in  $n_2$  estimation.

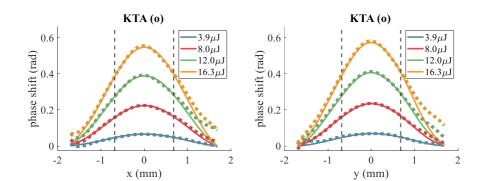


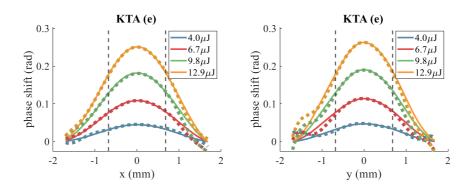


 $2.4 \mu J$ 

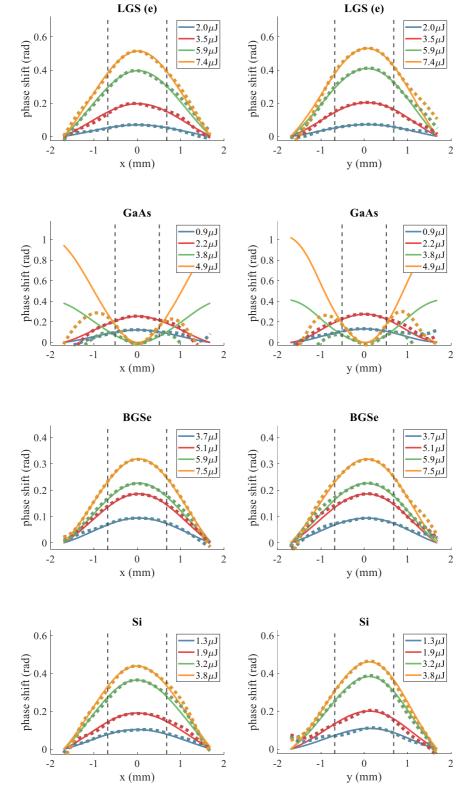
4.0μJ -6.6μJ -8.5μJ



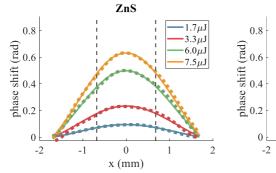


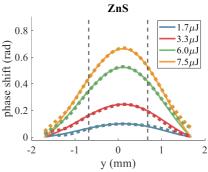


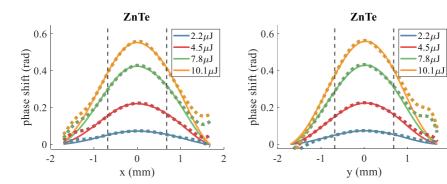
**Fig. S8.** Retrieved X and Y cuts of phase shifts observed in different samples for various laser pulse energies at 2.2  $\mu$ m. Dashed line - data, solid line - approximation. The vertical dashed lines indicate the part of the data included in  $n_2$  estimation.

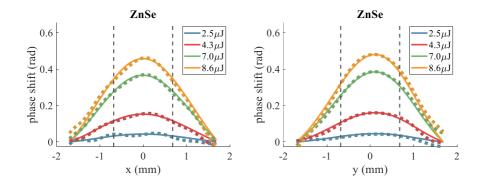


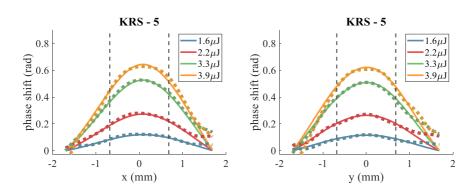
**Fig. S9.** Retrieved X and Y cuts of phase shifts observed in different samples for various laser pulse energies at 2.2  $\mu$ m. Dashed line - data, solid line - approximation. The vertical dashed lines indicate the part of the data included in  $n_2$  estimation.



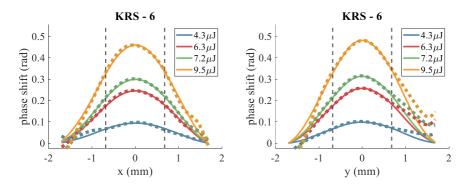




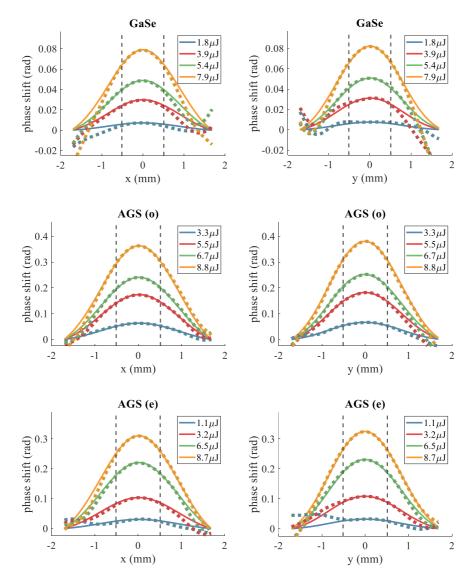




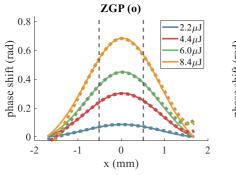
**Fig. S10.** Retrieved X and Y cuts of phase shifts observed in different samples for various laser pulse energies at 2.2  $\mu$ m. Dashed line - data, solid line - approximation. The vertical dashed lines indicate the part of the data included in  $n_2$  estimation.

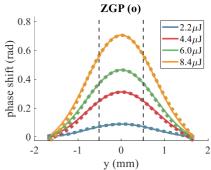


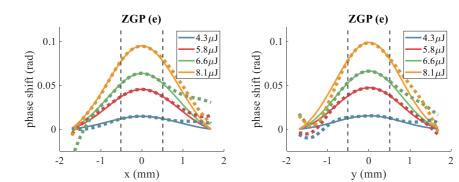
**Fig. S11.** Retrieved X and Y cuts of phase shifts observed in KRS-6 for various laser pulse energies at 2.2  $\mu$ m. Dashed line - data, solid line - approximation. The vertical dashed lines indicate the part of the data included in  $n_2$  estimation.

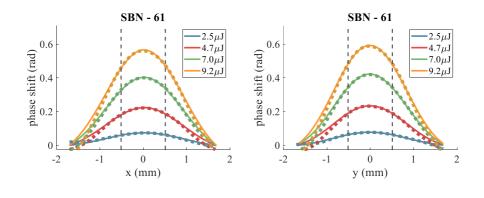


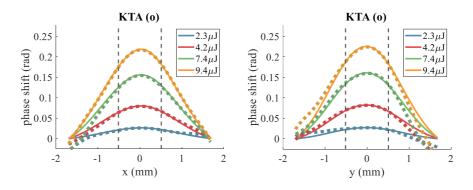
**Fig. S12.** Retrieved X and Y cuts of phase shifts observed in different samples for various laser pulse energies at 3.2  $\mu$ m. Dashed line - data, solid line - approximation. The vertical dashed lines indicate the part of the data included in  $n_2$  estimation.



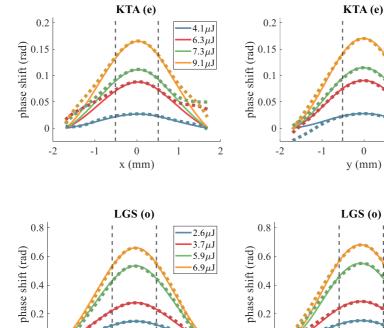








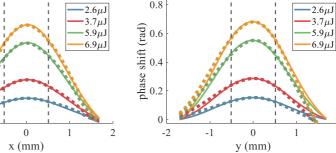
**Fig. S13.** Retrieved X and Y cuts of phase shifts observed in different samples for various laser pulse energies at 3.2  $\mu$ m. Dashed line - data, solid line - approximation. The vertical dashed lines indicate the part of the data included in  $n_2$  estimation.



0

-2

-1



4.1µJ

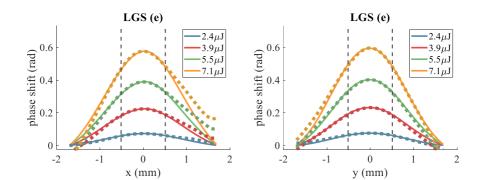
6.3µJ

 $7.3 \mu J$ 

**9**.1µJ

2

2



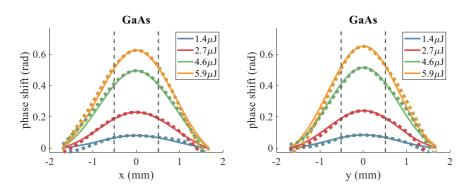
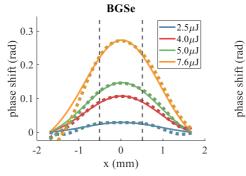
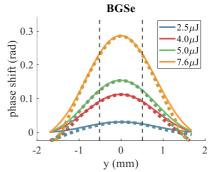
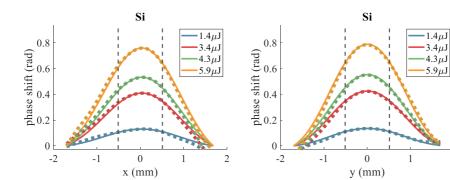
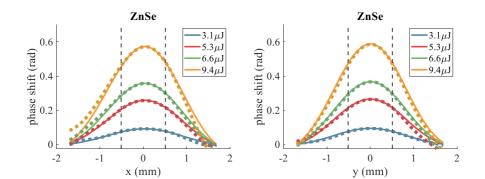


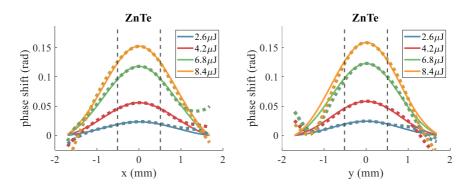
Fig. S14. Retrieved X and Y cuts of phase shifts observed in different samples for various laser pulse energies at 3.2 µm. Dashed line - data, solid line - approximation. The vertical dashed lines indicate the part of the data included in  $n_2$  estimation.



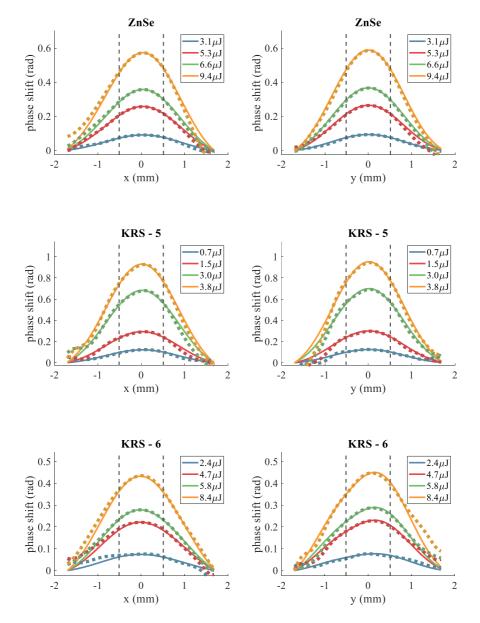








**Fig. S15.** Retrieved X and Y cuts of phase shifts observed in different samples for various laser pulse energies at 3.2  $\mu$ m. Dashed line - data, solid line - approximation. The vertical dashed lines indicate the part of the data included in  $n_2$  estimation.



**Fig. S16.** Retrieved X and Y cuts of phase shifts observed in different samples for various laser pulse energies at 3.2  $\mu$ m. Dashed line - data, solid line - approximation. The vertical dashed lines indicate the part of the data included in  $n_2$  estimation.

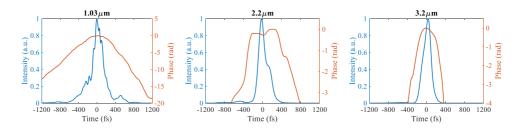


Fig. S17. Typical measured pulse shapes and phases for different wavelengths.

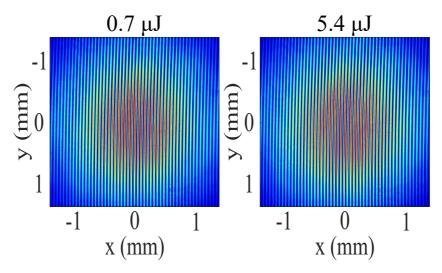


Fig. S18. Interference patterns, corresponding to the marginal energy values of the SBN-61 measurement at 1.03  $\mu$ m.

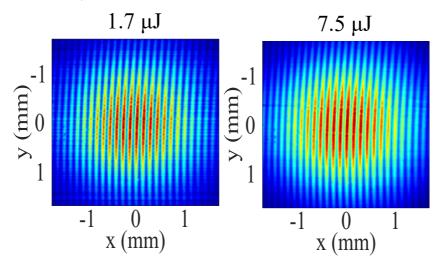


Fig. S19. Interference patterns, corresponding to the marginal energy values of the ZnS measurement at 2.2  $\mu \rm m.$ 

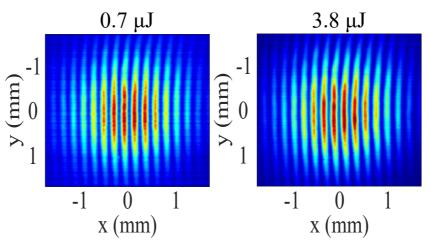
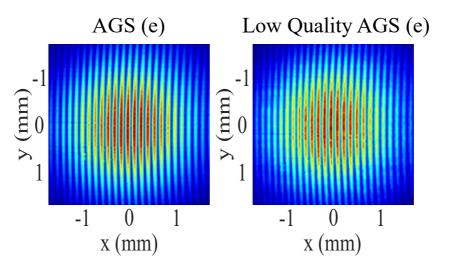
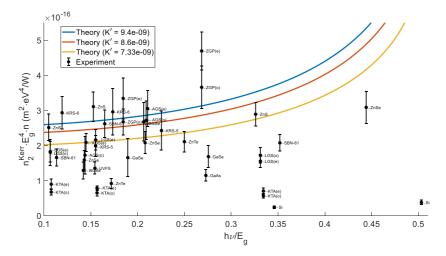


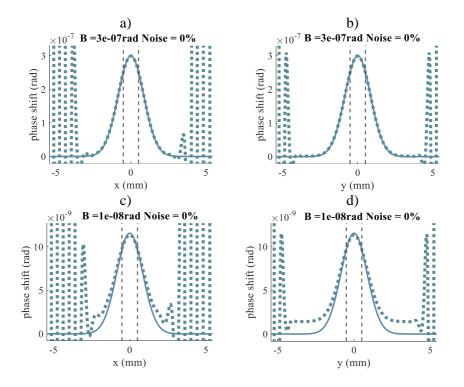
Fig. S20. Interference patterns, corresponding to the marginal energy values of the KRS-5 measurement at 3.2  $\mu$ m.



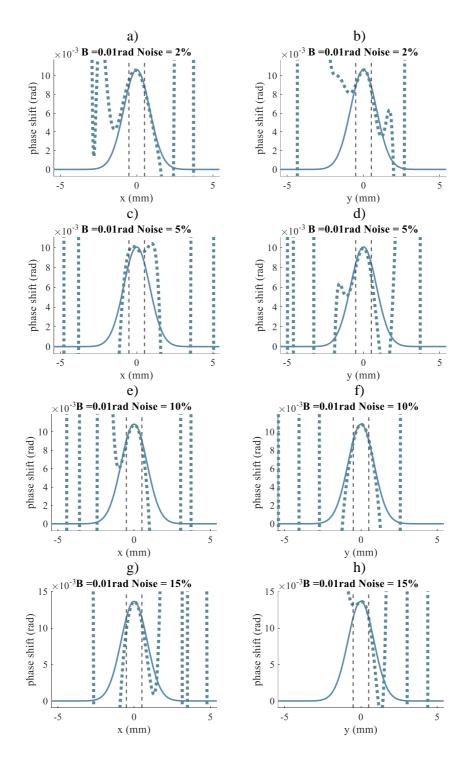
**Fig. S21.** Interference patterns for different quality samples of AGS (e) at 2.2  $\mu$ m. Measured with similar peak intensity and thickness.



**Fig. S22.** A comparison of our  $n_2^{\text{Kerr}}$  (where available) data with the two-band model. Here  $E_g$  - band gap energy, h - Planck's constant,  $\nu$  - frequency [Hz] of the photon and K' - parameter of the model. We used the value  $E_p = 21 \text{ eV}$  for calculations.



**Fig. S23.** Numerical simulation results addressing phase shift sensing capabilities of FTM. Dashed line - data, solid line - approximation. Vertical dashed lines indicate the fitting range. Parameters of the model: identical continuous wave Gaussian beams, beam radius at  $e^{-2}$  level - 1.7 mm,  $\lambda = 3.24 \ \mu$ m,  $\gamma = 1^{\circ}$ , 640x640 pixel matrix, pixel pitch - 17  $\mu$ m, no noise and B = (a,b)  $3 \cdot 10^{-7}$  rad, (c,d)  $10^{-8}$  rad. The fit range was  $\pm 0.51$  mm (the same as in real experiments using this wavelength). In case of b) the retrieved *B* had an error of 16 %.



**Fig. S24.** Numerical simulation results addressing phase shift sensing capabilities of FTM in the presence of noise. Noise in the simulations was of differing fraction of the signal amplitude. Dashed line - data, solid line - approximation. Vertical dashed lines indicate the fitting range. Parameters of the model: identical continuous wave Gaussian beams, beam radius at  $e^{-2}$  level - 1.7 mm,  $\lambda = 3.24 \,\mu$ m,  $\gamma = 1^{\circ}$ , 640x640 pixel matrix, pixel pitch - 17  $\mu$ m and B =  $10 \cdot 10^{-3}$  rad. The fit range was  $\pm 0.51$  mm (the same as in real experiments using this wavelength). The *B* retrieval error was 6 % (a,b), 1 % (c,d), 8 % (e,f) and (g,h) 37%.